

(Following Paper ID and Roll No. to be filled in your answer book)

Paper ID: XXXXXXXXXX

Roll No

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M.Tech
FIRST SEMESTER EXAMINATION, 2007-2008
ADVANCE CONTROL SYSTEM

Time: 3hrs.

Max. Marks:100

Note: Attempt any Five questions. All questions carry equal marks.

Q.1 Attempt any Two of the following:-

- (a) Determine the controllability and observability properties of the following systems (i) $A = \begin{bmatrix} -2 & 1 \\ 1 & -2 \end{bmatrix}$ $b = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ $c = \begin{bmatrix} 1 & -1 \end{bmatrix}$ (ii) $A = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ $b = \begin{bmatrix} 2 \\ 5 \\ 0 \end{bmatrix}$ $c = \begin{bmatrix} 0 & 1 \end{bmatrix}$.
- (b) Given a transfer function $G(s) = 10/s(s+1) = Y(s)/U(s)$
 Construct the state models for this system:
 (i) one which is both controllable and observable
 (ii) one which is controllable but not observable.
- (c) Derive the expression for the nth-order system characteristic polynomial; when conversion takes place from state variable model to transfer functions.

Q.2 Attempt any Two of the following:-

- (a) What is Liapunov function? State the stability and instability theorem of Liapunov with its equations.
- (b) Discuss in detail
 (i) Dead-Zone non-linearity
 (ii) Saturation non-linearity
 (iii) On-Off non-linearity with dead zone.
- (c) A system has matrix differential equation
 $\dot{x} = \begin{bmatrix} 0 & 1 & 2 & 0 \end{bmatrix} x + \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} u$
 What values for b_1 and b_2 are required so that the system is controllable?

Q.3 Attempt any **Two** of the following:-

- (a) Discuss the small gain theorem and robust stabilization in detail.
- (b) Write note on optimal control with an example.
- (c) Linearization of nonlinear systems

Q.4 Attempt any **Two** of the following:-

- (a) Write the statement of the sampling theorem. Draw the block diagram representation of the S/H device; also define the following (i) Acquisition Time (ii) Aperture Time (iii) Settling Time (iv) Hold-Mode Droop.
- (b) Define the z-transform. Establish the relationship between the Laplace transform and the z-transform.
- (c) Find the z-transform of the unit-step function $u_s(t)$ which is defined as

$$u_s(t) = 1 \quad t > 0$$
$$u_s(t) = 0 \quad t < 0.$$

Q.5 Write the short notes on the following:-

- (i) Robust control and system sensitivity
- (ii) Statement of Lure Problem
