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MCA**(SEM III) THEORY EXAMINATION 2017-18
DEGIN & ANALYSIS of ALGORITHMS****Time: 3Hours****Max. Marks: 100****Note:** Attempt all Sections. Assume missing data, if any.**SECTION-A****Q1. Attempt all parts of this question.****10x2=20**

- (a) Why Counting sort is called stable sort.
- (b) Apply BUCKET SORT algorithm on the following array $0 \cdot 78, 0 \cdot 17, 0 \cdot 39, 0 \cdot 26, 0 \cdot 72, 0 \cdot 94, 0 \cdot 21, 0 \cdot 21, 0 \cdot 12, 0 \cdot 23, 0 \cdot 68$
- (c) State the properties of Binomial Tress.
- (d) Differentiate between asymptotic notation O and Ω .
- (e) Define Hamiltonian cycle.
- (f) Explain randomized algorithm with the help of an example.
- (g) Differentiate between average analysis and amortized analysis.
- (h) Define NP problems.
- (i) What is time efficiency of Merge Sort Algorithm?
- (j) Find the time complexity of recurrence relation.

$$T_n = 2T_{\sqrt{n}} + 1$$

SECTION-B**Q2. Attempt any five questions.****10x5=50**

- (a) Use a Recursion tree/Master Method to give an asymptotic tight solution to the

$$T_n = 4T_{\frac{n}{2}} + n^2\sqrt{n}$$
- (b) What is amortized Analysis? Explain accounting method with the help of an example.
- (c) Write an algorithm to sort the given array of element using Quick-sort. Illustrate the operation of PARTITION procedure on the array = $\langle 2, 8, 7, 1, 3, 5, 6, 4 \rangle$.
- (d) Discuss the weighted union procedure for data structure for disjoint set and how to improve its worst case complexity.
- (e) Write & Explain Dijkstra's Algorithm with the help of suitable example.
- (f) Write & Explain Travelling Salesman problem.
- (g) Discuss the classess P, NP, NP complete and NP hard with examples.
- (h) Solve the all-pairs shortest Path problem for the digraph with the weight matrix given below:

	A	B	C	D
A	0	∞	∞	3
B	2	0	∞	∞
C	∞	7	0	1
D	6	∞	∞	0

SECTION-C**Attempt any two questions.****15x2=30**

Q3. Use Strassen's matrix multiplication algorithm to multiply the following two matrices:

$$A = \begin{pmatrix} 3 & 2 \\ 4 & 8 \end{pmatrix} \quad B = \begin{pmatrix} 1 & 5 \\ 9 & 6 \end{pmatrix}$$

What is its time complexity?

Q4. Differential between the following:

- (i) Depth First & Breadth first Search
- (j) Dynamic Programming & Divide/Conquer Approach.

Q5. Apply the Greedy method to solve the following instance of Knapsack problem. Item $n = 7$

Knapsack capacity $M = 15$, $P_1, P_2, \dots, P_7 = (10, 5, 15, 7, 6, 18, 3)$ & $\omega_1, \omega_2, \dots, \omega_7 = (2, 3, 5, 7, 1, 4, 1)$.