

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID: 7113

Roll No.

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MBA

(SEM ^{IV}~~IV~~) EVEN SEMESTER THEORY EXAMINATION, 2009-2010

OPERATIONS RESEARCH

Time : 3 Hours

Total Marks : 100

- Note : (i) Attempt all questions.
(ii) Question paper contain three sections.

SECTION - A

Attempt all questions :

1. Fill in the blanks with an appropriate word/phrase or formula. (10x1=10)
 - (a) Decision theory is concerned with decision making under condition of _____ .
 - (b) _____ is employed for taking decisions when regret matrix is used.
 - (c) The decision tree approach to decision making is used in situations where _____ are needed.
 - (d) The _____ enables the decision makers to decide whether or not to seek information.
 - (e) The solution to a problem is said to be degenerate if the number of occupied cells is _____ .
 - (f) If the saddle point does not exist, then the players have to employ _____ .
 - (g) In a Poisson - Exponential single server - infinite population model the expected number of customers in the queue is equal to _____ .
 - (h) In an assignment problem solution multiple zeros in all columns and rows are indication of _____ .
 - (i) If there are two (or more) critical paths in a given network, then the one with _____ should be used for determining the probability of completing the project in given time.
 - (j) The difference between the earliest start of the successor activity and the latest completion of the given activity is termed as _____ .

Attempt all questions :

2. Mark the following statements a T (True) or F (False). (10x1=10)
- (a) Every linear programming problem has a unique optimal solution.
 - (b) It is possible for the objective function value of an LPP to be the same at two distinct extreme points.
 - (c) The feasible region of a LPP must be a convex set.
 - (d) An LPP can have only two decision variables.
 - (e) To solve a LPP by simplex method it is essential that all variables in it to be non-negative.
 - (f) In improving a non optimal solution, the key element may be positive, negative or zero.
 - (g) A transportation problem is said to be unbalanced when the number of origins does not match with the number of destinations.
 - (h) A closed loop in a transportation problem would always involve an even number of cells.
 - (i) The relevant cost element is replaced by a zero in case a certain worker is not to be assigned a particular job.
 - (j) In a two person game, both the players must have an equal number of strategies.

SECTION - B

3. In a Game the organiser can hide the prize in one of five fox holes (1, 2, 3, 4 or 5) (see fig. 1). A gunner has a single shot and may fire at any of the four spots A, B, C or D. The gunner will win the prize if the prize is in a fox hole adjacent to the spot where the shot was fired. For example, a shot fired at spot B, the gunner wins the prize if prize is in foxhole 2 or 3.
- (a) Assuming this to be a zero - sum game, construct the reward matrix. (8)
 - (b) Find and eliminate all dominated strategies. (4)
 - (c) Write down each player's LP. (6)
 - (d) Find the optimal strategy and value of the game. (12)



Figure-1

OR

- (a) Given the following network and activity time estimate, determine the expected project completion time and variance. (12)

| ACTIVITY | Time estimates (DAYS) | | |
|----------|-----------------------|----|----|
| | to | tm | tp |
| 1 - 2 | 5 | 8 | 17 |
| 1 - 3 | 7 | 10 | 13 |
| 2 - 3 | 3 | 5 | 7 |
| 2 - 4 | 1 | 3 | 5 |
| 3 - 4 | 4 | 6 | 8 |
| 3 - 5 | 3 | 3 | 3 |
| 4 - 5 | 3 | 4 | 5 |

(b) A businessman has two independent investments A and B available to him, but he lacks capital to undertake both of them simultaneously. He can choose to take A first and then stop, or if A is successful then take B, or vice versa. The probability of success on A is 0.7 while for B it is 0.4. Both investment require an initial capital outlay of Rs. 2000, and both return nothing if the venture is unsuccessful. Successful completion of A will return Rs. 3000/- (over cost), successful completion of B will return Rs. 5000/- (over cost). Draw the decision tree and determine the best strategy.

(c) Write the dual of the following primal problem : (6)

$$\text{Maximize } Z = -5x_1 + 2x_2.$$

Subject to :

$$x_1 - x_2 \geq 2$$

$$2x_1 + 3x_2 \leq 5$$

$$x_1, x_2 \geq 0$$

SECTION - C

4. Attempt any two of the following : (12½)

- (a) Explain the scope and methodology of Operation Research.
- (b) Discuss the difference between decision making under certainty and decision making under uncertainty.
- (c) Describe the meaning of EMV and EVPI.

5. Attempt any two of the following : (12½)

- (a) Discuss the role of sensitivity analysis in linear programming.
- (b) Using Vogel's Approximation Method, find the basic feasible solution of the following transportation problem.

| | D1 | D2 | D3 | D4 | Availability |
|--------------|----|----|----|----|--------------|
| S1 | 19 | 30 | 50 | 12 | 7 |
| S2 | 70 | 30 | 40 | 60 | 10 |
| S3 | 40 | 10 | 60 | 20 | 18 |
| Requirements | 5 | 8 | 7 | 15 | |

(c) Four jobs are to be done on four different machines. Assign the jobs so as to maximize the total profit.

| | M1 | M2 | M3 | M4 |
|----|----|----|----|----|
| J1 | 15 | 11 | 13 | 15 |
| J2 | 17 | 12 | 12 | 13 |
| J3 | 14 | 15 | 10 | 14 |
| J4 | 16 | 13 | 11 | 17 |

6. Attempt any two of the following :

(12½)

(a) Solve the following game whose pay off is given by :

| | | | | |
|----------------|----------------|----------------|----------------|----------------|
| | B ₁ | B ₂ | B ₃ | B ₄ |
| A ₁ | 1 | 7 | 3 | 4 |
| A ₂ | 5 | 6 | 4 | 5 |
| A ₃ | 7 | 2 | 0 | 3 |

(b) We have five jobs, each of which must be processed on the two machine A and B in order AB. Processing time in hours are given in the table below :

Determine a sequence for the five jobs that will minimize the elapsed time T.

| | | | | | |
|-------------|---|---|---|---|----|
| Job : | 1 | 2 | 3 | 4 | 5 |
| Machine A: | 5 | 1 | 9 | 3 | 10 |
| Machine B : | 2 | 6 | 7 | 8 | 4 |

(c) Use the graphical method to minimize the time needed to process the following jobs on the machine shown. Also calculate the total elapsed time to complete both jobs.

| | | | | | |
|----------------|---------|---|---|---|---|
| | Machine | | | | |
| Job 1 Sequence | A | B | C | D | E |
| Time (hrs) | 3 | 4 | 2 | 6 | 2 |

| | | | | | |
|----------------|---------|---|---|---|---|
| | Machine | | | | |
| Job 2 Sequence | B | C | A | D | E |
| Time (hrs) | 5 | 4 | 3 | 2 | 6 |

7. Attempt any two of the following :

(12½)

- (a) Give a general structure of queuing system and explain.
- (b) Briefly explain the costs which are relevant to decisions for replacement of depreciable assets.
- (c) Briefly discuss Resource levelling and Resource smoothing while managing a project.