

- (b) Use the window design method to design a minimum-order high-pass filter with a stop band cut-off frequency $w_s = 0.22\pi$, a passband cut-off frequency $w_p = 0.28\pi$ and a stop band ripple $\delta_s = 0.003$.
- (c) Use the Impulsive Invariance method to design a digital filter from an analog prototype that has a system function

$$H_a(s) = \frac{s+a}{(s+a)^2 + b^2}$$

5. Answer any two of the following : 10x5=20

- (a) Write notes on :
 - (i) Goertzel algorithm
 - (ii) Effect of finite register length.

(b) Compute the eight point DFT of the sequence :

$$X(n) = \begin{cases} 1, & 0 \leq n \leq 7 \\ 0, & \text{otherwise} \end{cases}$$

By using the decimation-in-frequency FFT algorithm.

(c) How spectrum analysis of random signals are performed using estimates of the auto-correlation sequence?

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Printed Pages : 4



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EEN-011

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 121657

Roll No.

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B.Tech

(SEM VI) THEORY EXAMINATION 2015
FUNDAMENTALS OF DIGITAL SIGNAL
PROCESSING (EEN 011)

Time : 3 Hours]

[Total Marks : 100

Note: 1. Attempt all questions:

2. All question carry equal marks.

1. Answer any **Four** of the following: (5x4=20)

(a) Find the even and odd parts of the signal $X(n)=u(n)$.

(b) A Linear discrete-time system is characterized by its response $h_k(n)$ to a delayed unit sample $\delta(n-k)$. determine whether or not the system $h_k(n) = \delta(2n-k)$ is shift-invariant.

(c) Find the DIFT of $\delta(n)$.

(d) State and Prove the Periodicity and Symmetry properties of DFT.

(e) Find the convolution of two signals:

$$X(n) = a^n u(n) \quad \text{and} \quad h(n) = u(n)$$

(f) How the Discrete Cosine Transform (DCT) is obtained from DFT? Explain.

2. Answer any **Two** of the following : (10x2=20)

(a) Explain the discrete-time processing of analog signals.

(b) State and prove the sampling theorem. If the Nyquist rate for $X_a(t)$ is w_s , what will be the Nyquist rate for signal $\frac{dx_a(t)}{dt}$.

(c) (i) Write short note on multi rate signal processing.

(ii) Consider the discrete-time sequence $x(n) = \cos\left(\frac{nr}{8}\right)$. Find two different continuous-time signals that would produce the sequence when sampled at a frequency of $f_s = 10 \text{ Hz}$.

3. Answer any **Two** of the following: (10x2=20)

(a) If a input to a linear shift- invariant system is

$$X(n) = \left(\frac{1}{2}\right)^n u(n) + 2^n u(-n-1)$$

The output is

$$Y(n) = 6 \left(\frac{1}{2}\right)^n u(n) - 6 \left(\frac{3}{4}\right)^n (n). \text{ Find the system function}$$

and determine whether or Not the system is stable and/ or casual. Also comment on the realizability of system.

(b) Evaluate the frequency response of the system

described by the system function $H(z) = \frac{1}{1-0.8Z^{-1}}$ after deriving expression for frequency response of a system with Rational function.

(c) Comment on the following :

(i) Finite precision numerical effects

(ii) Effects of round of noise in digital filters.

4. Answer any **Two** of the following: (10x2=20)

(a) Design a low-pass Butterworth filter having following specifications:

$$\therefore f_p = 6\text{kHz}, f_s = 10\text{kHz}, \delta_p = \delta_s = 0.1$$