

BTECH
(SEM-III) THEORY EXAMINATION 2018-19
BASIC SYSTEM ANALYSIS

Time: 3 Hours**Total Marks:100****Notes: Assume any Missing Data.****SECTION – A****(1) Attempt all parts. Each part carries equal marks. (10×2= 20)**

- (a) Write properties of Z-transform.
- (b) Define unit steps and unit ramp signals with proper sketch.
- (c) Determine whether or not signal $x(t) = \cos \frac{2\pi n}{7} \sin \frac{3\pi n}{14}$ is periodic. If periodic find its fundamental period.
- (d) Write Dirichlet's condition for the existence of Fourier series.
- (e) Sketch the signal $y(t) = r(t+2) - r(t) + r(t-2)$.
- (f) Find Z-transform of unit step and impulse function.
- (g) Find the Laplace transform of $\cos \omega t$.
- (h) Define State and State variable.
- (i) Write the properties of ROC.
- (j) Define STM..

SECTION – B**(2) Attempt any three questions. Each question carries equal mark (10×3= 30)****(a) Determine the Fourier transform of the following function.**

(i) $f(t) = e^{-at}$ for all value of t

(ii) $f(t) = 1, -\infty < t < \infty$

(iii) Unit impulse function,

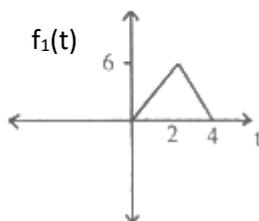
(b) Find the Laplace transform of the waveforms as shown in fig. 1 & 2.

Fig. 1

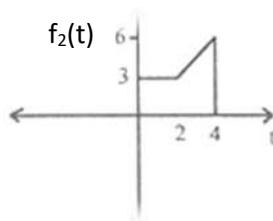


Fig. 2

(c) Determine Z-Transform of the following sequences with ROC

(i) $x(n) = \left(\frac{1}{2}\right)^n ; 0 \leq n \leq 6$

$x(n) = 0 ; \text{ otherwise}$

(ii) $x(n) = n^2 u(n) + nu(n)$

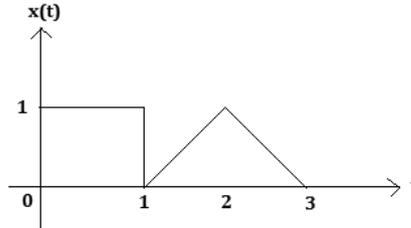
(d) A second-order Discrete Time system is described by the difference equation

$$y(n) - 3y(n-1) + y(n-2) = x(n)$$

Determine: -

- (i) $H(z)$, the system function,
- (ii) $h(n)$, the unit-impulse response.

(e) Sketch (i) $x(-\frac{t}{2} + 2)$ & (ii) $x(-2t - 3)$ if $x(t)$ is



Section – C

(3) Attempt any **one** question.

(10×1= 10)

(a) A vector matrix differential equation of a system is given by

$$\dot{X} = \begin{bmatrix} 0 & 1 \\ -6 & 5 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

$$\text{and output } Y = [1 \ 0] X$$

With initial conditions being zero. Find time response of the above system.

(b) Find the state transition matrix for the system matrix having

$$A = \begin{bmatrix} 0 & -1 \\ 2 & -3 \end{bmatrix}$$

(4) Attempt any one question.

(10×1= 10)

(a) Find the inverse Z-transform of the following function:

$$(i) X(Z) = \frac{1 - \frac{1}{3}Z^{-1}}{(1 - Z^{-1})(1 - 2Z^{-1})} \quad |Z| > 2$$

$$(ii) X(Z) = \frac{1 - \frac{5}{6}Z^{-1}}{(1 - \frac{1}{4}Z^{-1})(1 - \frac{1}{3}Z^{-1})} \quad |Z| > \frac{1}{3}$$

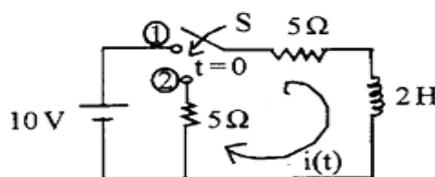
(b) Prove convolution theorem of Z-transform.

(5) Attempt any one question.

(10×1= 10)

(a) In the circuit shown in figure, determine the current $i(t)$ when the switch is at position 2. The switch

S is moved from position 1 to position 2 at $t=0$. Initially the switch is at position 1 for a long time.



(b) State and prove initial and final value theorem of Laplace transform.

(6) Attempt any one question.

(10X1=10)

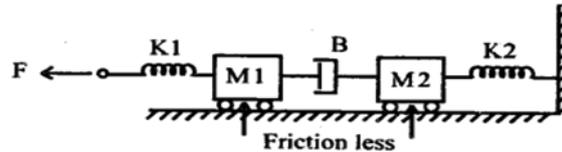
(a) Find trigonometric Fourier series representation of $x(t) = e^{at} u(t)$.

(b) State and prove duality property of Fourier transform.

(7) Attempt any one question.

(10X1=10)

(a) Write mechanical balanced force equation & draw electrical analogous by the force voltage analogy of given mechanical system



(b) What are the properties of continuous time linear system? Consider a continuous time system, the input and output is related by $y(t)=t^2(t-1)$. Determine whether the system is linear or non-linear.