



Printed Pages : 4

TEE-301

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 2047

Roll No.

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B. Tech.**(SEM. III) EXAMINATION, 2007-08****BASIC SYSTEM ANALYSIS***Time : 3 Hours**[Total Marks : 100**Note : Attempt all questions.*1 Attempt any **four** parts of the following : **5×4=20**(a) Calculate energies and powers of the following **5**
signals :(i) $e^{-5t}u(t)$ (ii) $2 \sin 2t + 3 \cos \pi t$ (b) Calculate the following integrals : **5**

(i)
$$\int_{-\infty}^5 (5 + \cos t) \delta(t - 10) dt$$

(ii)
$$\int_{-\infty}^{\infty} (t - 2)^2 \delta(t - 2) dt$$

(iii)
$$\int_{-\infty}^{\infty} e^{-at^2} \delta(t - 10) dt$$

(c) Differentiate between time-invariant and **5**
time-variant systems. Give a suitable example for
both types of systems.(d) What do you understand by linear systems ? **5**
Show that the system described by the following
differential equation is linear

$$\dot{y}(t) + t y(t) = r(t)$$



- (e) Sketch the waveforms of the following signals : 5
- (i) $x(t) = u(t) - u(t - 2)$
 - (ii) $x(t) = u(t + 1) - 2u(t) + u(t - 1)$
 - (iii) $y(t) = r(t + 1) - r(t) + r(t - 2)$
- where $u(t)$ and $r(t)$ are unit step and ramp signals respectively.
- (f) Consider the R-L-C series circuit in Fig. 1 which 5 is closed at $t = 0$. Write the loop equation for this circuit assuming zero initial condition. What are three different possible situations of the transient solution of above equations? Describe the corresponding relationship R, L and C for each of the situations.

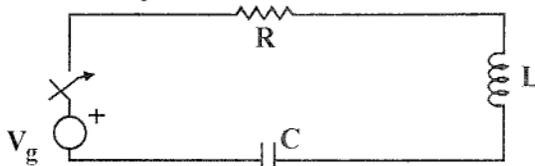


Fig. 1

- 2 Attempt any two parts of the following : 2×10=20
- (a) Determine the effect of each of the following 10 symmetry conditions on the coefficients of the Fourier series expansion for $f(\theta)$ and obtain the formula for those coefficients which do not vanish
 - (1) $f(\theta) = f(\pi - \theta)$
 - (2) $f(\theta) = -f(\pi - \theta)$
 - (b) What are Dirichlet's conditions? 10
 - (1) Find the Fourier transform of $x(t) = \delta(t)$
 - (2) Find the inverse Fourier transform of $X(jw) = 2\pi \delta(w)$.
 - (c) Find the Fourier series of the signal shown in 10 Fig. 2. using exponential form.

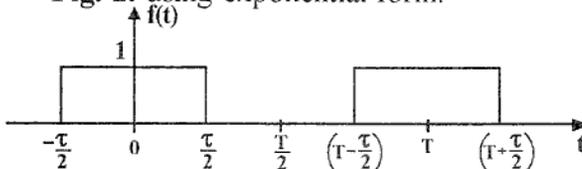


Fig. 2



3 Attempt any **two** parts of the following : $2 \times 10 = 20$

- (a) Use the Laplace transform to determine the output of a system represented by the differential equation 10

$$\ddot{y}(t) + 5 \dot{y}(t) + 6y(t) = 2\dot{x}(t) + x(t)$$

in response to the input $x(t) = u(t)$. Assume that all initial conditions are zero.

- (b) Prove the following results : 10

$$(1) \quad L \left[y \left(\frac{t}{a} \right) \right] = a Y(s), \quad a > 0$$

$$(2) \quad L [ty(t)] = \frac{d}{ds} Y(s)$$

where $Y(s)$ is Laplace transform of $y(t)$. 10

- (c) Find the Laplace transform of the wave form shown in Fig 3. It is to be noted that $v(t) = 0$ for $t > 2T$ and $t < 0$.

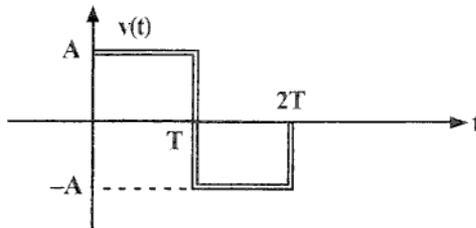


Fig. 3

4 Attempt any **two** parts of the following : $2 \times 10 = 20$

- (a) Find the state transition matrix for 10

$$A = \begin{bmatrix} 0 & 1 \\ -6 & -5 \end{bmatrix}$$

Find the corresponding resolvent matrix also.

- (b) Find the output response of the system 10
described by the following state variable formulation.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t) \quad \text{to unit step input}$$

It is given that $C = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ and $x^T(0) = [1 \ 1]$.

- (c) Consider the state variable model of a 10
second-order system represented as

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 2 \end{bmatrix} r$$

$$\begin{bmatrix} x_1(0) \\ x_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix}; \quad r = \text{unit step.}$$

Find the state response $x(t)$, $t > 0$

- 5 Attempt any **two** parts of the following : 2×10=20

- (a) Find the Z -transform of the sequences 10

(i) $\delta(k)$ (ii) $u(k)$ (iii) $e^{\pm\beta k}$; $k \geq 0$

- (b) Prove that $\lim_{z \rightarrow \infty} F(z) = f(0)$ 10

$$\lim_{k \rightarrow \infty} f(k) = \lim_{z \rightarrow 1} \left[\left(\frac{z-1}{z} \right) F(z) \right]$$

where $F(z)$ is Z transform of $f(k)$.

- (c) Obtain the Z -inverse of $F(z)$ for the following : 10

(1) $\frac{z}{(z-0.4)}$, $|z| > 0.4$

(2) $\frac{Z}{(z-0.4)}$, $|z| < 0.4$

