

B.Tech
(SEM V) THEORY EXAMINATION 2018-19
FUNDAMENTALS OF EM THEORY

Time: 3 Hours

Total Marks: 100

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

1. Attempt *all* questions in brief 2 x 10 = 20

- a. What is Gauss law?
- b. What do you mean by irrotational and solenoidal field?
- c. Define equipotential surface.
- d. Write the differences between convection current and conduction current.
- e. Define dielectric strength.
- f. Explain the concept of vector magnetic potential.
- g. What is Lenz's law?
- h. Define intrinsic impedance and phase velocity.
- i. Explain reflection coefficient and transmission coefficient.
- j. What is dispersion?

SECTION B

2. Attempt any *three* of the following: 10 x 3 = 30

- a. Discuss the physical significance of gradient, divergence and curl. Also state and prove Stoke's theorem.
- b. What do you mean by scalar and vector fields? Transform a vector function $\mathbf{B} = y\mathbf{a}_x - x\mathbf{a}_y + z\mathbf{a}_z$ into cylindrical system.
- c. Write down Poisson's and Laplace's equations in cylindrical coordinate system. Consider two concentric spheres of radii a and b , $a < b$. The outer sphere is kept at a potential V_0 and the inner sphere at zero potential. Solve Laplace equation in cylindrical coordinates to find
 - (i) The potential and electric field in the region between two spheres.
 - (ii) Find the capacitance between them.
- d. What is Ampere's law? Derive an expression for magnetic field intensity due to long hollow conducting cylinder.

- e. What is uniform plane wave? A 10 GHz plane wave travelling in free space has an amplitude of $E_x = 10$ V/m. Find v , λ , β , η and the amplitude and direction of H .

SECTION C

- 3. Attempt any one part of the following: 10 x 1 = 10**
- a. A total charge of 10^{-8} C is distributed uniformly along a ring of radius 5 m. Calculate the potential on the axis of the ring at a point 5 m from the centre of the ring. If the same charge is uniformly distributed on a disc of 5 m radius what will be the potential on its axis at 5 m from the centre.
- b. An infinite long line charge of uniform density ρ_L coulombs/cm is situated along the z - axis. Obtain electric field intensity due to this charge using Gauss law.
- 4. Attempt any one part of the following: 10 x 1 = 10**
- a. Explain the phenomenon of polarization in dielectric material. Determine the energy stored in the electric field in a concentric spherical shell.
- b. Write the properties of perfect conductors. Find the magnitude of the electric field intensity in a sample of silver having $\sigma = 6.17 \times 10^7$ mho/m and $\mu_e = 0.0056$ m²/V-s if :
- (i) The drift density is 1 mm/s
 (ii) The current density is 10^7 A/m²
 (iii) The sample is a cube, 3 mm on a side, carrying a total current of 80A
 (iv) The sample is a cube, 3 mm on a side, having a potential difference of 0.5 mV between opposite faces.
- 5. Attempt any one part of the following: 10 x 1 = 10**
- a. Verify divergence theorem for a vector field $\vec{A} = 3x\mathbf{a}_x + (3y+z)\mathbf{a}_y + (3z-x)\mathbf{a}_z$ in the region bounded by the cylinder $x^2 + y^2 = 9$ and the planes $x=0$, $y=0$, $z=0$ and $z=2$
- b. State and explain Biot-Savart law. Also derive an expression for the magnetic field intensity due to infinite long straight filament.

6. Attempt any *one part* of the following:

10 x 1 = 10

- a. What is the physical significance of displacement current? Also derive the equation of continuity for time varying fields.
- b. State and explain Maxwell's equation in differential and integral form. Also write the physical significance of Maxwell's equation.

7. Attempt any *one part* of the following:

10 x 1 = 10

- a. Derive a relation between vector E and vector H in uniform plane wave.
- b. In region 1, $y < 0$, $\epsilon_1 = 10 \text{ p F/ m}$, $\mu_1 = 2.35\mu \text{ H/m}$ and $\sigma_1 = 0$, for region 2, $y > 0$, $\epsilon_2 = 9 \text{ p F/ m}$, $\mu_2 = 4\mu \text{ H/m}$ and $\sigma_2 = 0$. An incident uniform plane wave in region 1 having electric field strength of $500 e^{-\gamma y} \text{ V/m}$ travelling towards the boundary at $y=0$. Find
 - (i) Total electric field intensity in region 1, (incident+ reflected) as a function of time.
 - (ii) Magnetic field intensity in region 2, as a function of time