

**B. TECH.**

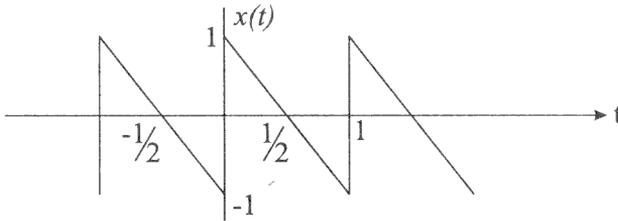
**FOURTH SEMESTER EXAMINATION, 2003-2004**  
**SIGNALS AND SYSTEMS**

Time : 3 Hours

Total Marks : 100

**Note :** Attempt **ALL** questions.1. Attempt any *FOUR* of the following :— (5×4)

- (a) Find the fundamental period  $T$ , the fundamental frequency  $\omega_0$  and the Fourier series coefficient  $a_k$  of the following periodic signal  $x(t)$  :—



- (b) Compute the DFT of the four-point sequence :

$$x(n) = (0; 1; 2; 3).$$

- (c) Show that if a discrete LTI system  $h(n)$  is subjected to input sequence  $x(n)$ , then its response  $y(n)$  is represented as :

$$y(n) = x(n) * h(n).$$

- (d) Show that

(i)  $\delta(n) = U(n) - U(n-1)$

(ii)  $u(n) = \sum_{k=0}^{\infty} \delta(n-k)$

(iii) Any signal can be decomposed into even and odd components. Explain with an example.

(e) Explain the Shift property and Duality property of Fourier series.

(f) Discuss the significance of :

(i) Impulse function,

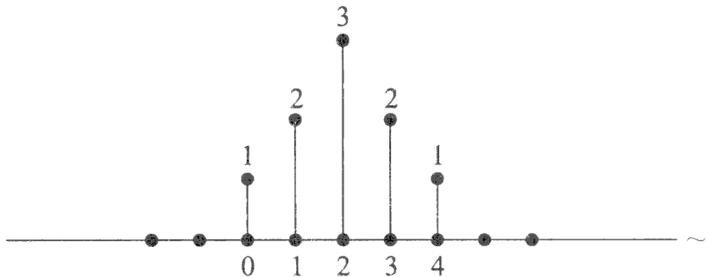
(ii) Unit step function,

(iii) Sinc function.

2. Attempt any *FOUR* of the following :— (5×4)

(a) A low pass digital filter with a sampling  $T = 50 \mu\text{s}$  has a cut off frequency 10 kHz. If the value of  $T$  in this filter changed to  $25 \mu\text{s}$ , determine the new cut off frequency of the filter. Repeat the problem if  $T$  is changed to  $100 \mu\text{s}$ .

(b) Consider a non-recursive filter with the impulse response shown in the figure. What is the group delay as a function of frequency for this filter ?



(c) What is understood by :

(i) Natural Response,

(ii) Forced response of a LTI system ?  
Explain with one appropriate example.

- (d) Differentiate between :
- (i) Ideal and Non-ideal filters,
  - (ii) IIR and FIR filters.
- (e) Write the S domain transfer function of a first order system. Sketch and interpret its magnitude and phase response as a function of frequency.
- (f) Find the convolution of the sequences :

$$x_1(n) = [1, \underset{\uparrow}{2}, 0] ; \quad x_2(n) = [2, \underset{\uparrow}{2}, 2]$$

3. Attempt any TWO of the following :— (10×2)

- (a) The random processes  $x(t)$  and  $y(t)$  are defined as :

$$\begin{aligned} x(t) &= V_1(t) + 3V_2(t-z) \\ y(t) &= V_2(t+z) + 3V_1(t-z), \end{aligned}$$

where  $V_1(t)$  and  $V_2(t)$  are independent white noise processes each with variance equal to 0.5. What are the autocorrelation functions of  $x$  and  $y$ ? Are these processes wide-sense stationary?

- (b) The independent random variables  $x$  and  $y$  have the probability densities :

$$\begin{aligned} f(x) &= e^{-x}; \quad 0 \leq x < \infty \\ f(y) &= 2e^{-2y}; \quad 0 \leq y < \infty \end{aligned}$$

Find and plot the probability density of the variable  $z = x+y$ .

(c) Explain the following terms :—

(i) Probability

(ii) Ergodic Process

(iii) Power spectral density of a random process

4. Attempt any TWO of the following :— (10×2)

(a) (I) Determine the Nyquist sampling rate and the Nyquist sampling interval for the following :—

(i)  $\text{Sinc}(100\pi t) + \text{Sinc}(50\pi t)$

(ii)  $\text{Sinc}(50\pi t) \text{Sinc}(100\pi t)$

(II) Explain Aliasing. What can be done to reduce aliasing ?

(b) What is understood by reconstruction of a continuous time signal from its samples known as interpolation? How is this reconstruction accomplished and what are the practical difficulties ?

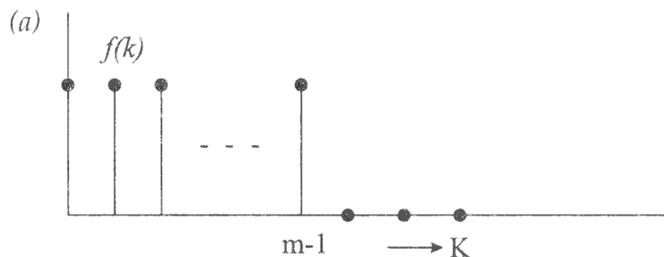
(c) Explain the following with reference to discrete time system :—

(i) Decimation or Down sampling

(ii) Interpolation or Up sampling

(iii) Time Shifting

5. Attempt any TWO of the following :— (10×2)



For the discrete time signal shown above, show that

$$F[Z] = \frac{1 - Z^{-m}}{1 - Z^{-1}}.$$

- (b) (i) Find the transfer function of a Unit Delay.
- (ii) Determine the system function for the causal LTI system with difference equation

$$y(n) - \frac{1}{2}y(n-1) + \frac{1}{4}y(n-2) = x(n).$$

- (c) Explain the following with reference to z-transform :—
- (i) Scaling property
- (ii) Convolution property
- (iii) Region of convergence of  $F(Z)$
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