

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 1075

Roll No.

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B.Tech.

(SEM. V) ODD SEMESTER THEORY

EXAMINATION 2010-11

DESIGN AND ANALYSIS OF ALGORITHMS

Time : 3 Hours

Total Marks : 100

- Note :** (1) Attempt **all** questions.
(2) All questions carry equal marks.

1. Attempt any **four** parts of the following :— **(5×4=20)**
- (a) Determine the asymptotic order of the following functions :
- (i) $f(n) = 6 \cdot 2^n + n^2$.
(ii) $f(n) = 7$.
- (b) Solve the recurrence relation $T(n) = 2T(\sqrt{n}) + 1$ whenever n is a perfect square greater than 1 and $T(2) = 3$.
- (c) Solve the recurrence relation using Master's Theorem :
 $T(n) = 7T(n/2) + 18n^2$, where $n \geq 2$ and a power of 2.
- (d) Write quick sort algorithm. Prove that the running time complexity of quick sort is $O(n \log n)$ in average.
- (e) You are given an array of n integers $a_1 < a_2 < \dots < a_n$. Give an $O(\log n)$ algorithm that finds index i where $a_i = i$ or prove that such i does not exist.
- (f) Describe Heap sort algorithm.

2. Attempt any two parts of the following: — (10×2=20)

(a) Show the Red black tree ~~that is in the~~ resulted after successively inserting the keys ~~11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100~~ 12, 19, 8 into an initially empty red black ~~tree~~

(b) Define a B-tree of order ~~m~~ m and let n be the number of elements in the B-tree. Show that

$$2^{h-1} - 1 \leq n \leq m^h - 1$$

where h is the height of the B-tree

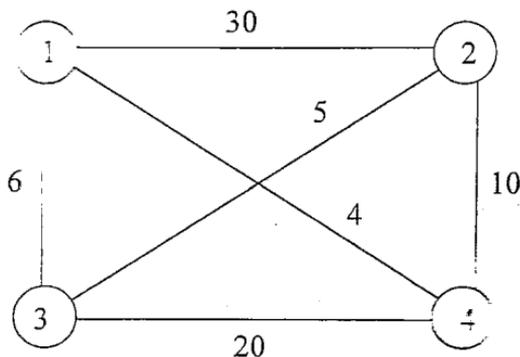
(c) Define Fibonacci heap. ~~Define Binomial~~ and Fibonacci heap.

3. Attempt any two parts of the following: — (10×2=20)

(a) Describe greedy method. Find the optimal solution to the Knapsack instance $n = 3$, $W = [100, 14, 10]$, $P = [20, 18, 15]$ and $C = 116$ using greedy method.

(b) Obtain the dynamic programming recurrence equations for the 0/1 Knapsack problem of n instances. Assume suitable data for n instances Knapsack.

(c) Consider a four vertex network as shown below. Find a least cost tour using backtracking method.

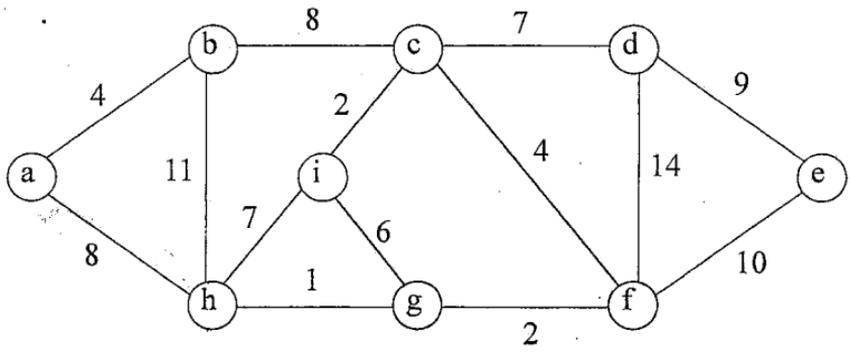


4. Attempt any **two** parts of the following :— (10×2=20)

(a) Use Strassen's algorithm to compute the product of two given matrices :

$$\begin{bmatrix} 1 & 3 \\ 5 & 7 \end{bmatrix} \text{ and } \begin{bmatrix} 8 & 4 \\ 6 & 2 \end{bmatrix}.$$

(b) Find the minimum cost spanning tree of the given graph using Prim's algorithm.



(c) Describe Floyd Warshal's algorithm to find all pairs shortest paths in a directed network.

5. Write short notes on any **four** of the following :— (5×4=20)

- (a) NP-Completeness.
- (b) Randomized algorithms.
- (c) Branch-and-Bound algorithm.
- (d) Approximation algorithms.
- (e) Hamiltonian cycle problem.
- (f) Chromatic Number.