



(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 9967

Roll No.

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B. Tech.

**(SEM. III) EXAMINATION, 2008-09
COMPUTER BASED NUMERICAL &
STATISTICAL TECHNIQUES**

Time : 3 Hours]

[Total Marks : 100

Note : (1) Attempt all questions.

(2) All questions carry equal marks.

1 Attempt any **four** of the following : 5×4(a) Let $f(x) = x^{-\frac{1}{10}}$ be computed for $0 \leq x \leq 10$

If x^* approximate x correct to n significant decimal digits, then to how many significant digits $f(x^*)$ approximate $f(x)$.

(b) Expand $\log(1+x)$ in a Taylor expansion about $x_0 = 1$ through terms of degree 4. Obtain a bound on the truncation error when approximating $\log(1.2)$ using this expansion.



(c) Find the root of the equation $2x = \cos x + 3$ correct to three decimal places by the iteration method.

(d) Show that the equation

$$f(x) = \cos\left(\frac{\pi(x+1)}{8}\right) + 0.148x - 0.9062 = 0$$

has one root in the interval $(-1, 0)$ and one in $(0, 1)$. Calculate the negative root correct to4 decimals by **Newton-Raphson** method.

(e) Show that the following sequence has convergence of the second order with same limit \sqrt{a}

$$x_{n+1} = \frac{1}{2} x_n \left(1 + \frac{a}{x_n^2} \right)$$

(f) Find the root of the equation $x^3 - 2x - 5 = 0$ which lies between 2 and 3 by Muller's method.



2 Attempt any **four** of the following . 5×4

(a) Prove the following

$$\Delta = \frac{1}{2} \delta^2 + \delta \sqrt{1 + \frac{\delta^2}{4}}$$

(b) Evaluate from following table $f(3.8)$ to three significant figures, using Gregory-Newton backward interpolation formula :

$x:$	0	1	2	3	4
$f(x):$	1.00	1.50	2.20	3.10	4.60

(c) From the following table, find the value of $e^{1.22}$ using Gauss's backward formula :

$x:$	1.00	1.05	1.10	1.15	1.20	1.25	1.30
$e^x:$	2.7183	2.8577	3.0042	3.1582	3.3201	3.4903	3.6693

(d) Using Stirling's formula, find $f(1.42)$ from the following table :

$x:$	1.0	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8
$f(x):$	0.84	0.89	0.93	0.96	0.99	1.01	1.02	1.03	1.04

(e) For the following table find $f(x)$ as a polynomial in x using Newton's divided difference formula .

$x:$	-1	0	3	6	9
$f(x):$	3	-6	39	822	1611

(f) Using Lagrange's interpolation formula, find $y(10)$ from the following table :

$x:$	5	6	9	11
$y:$	12	13	14	16

3 Attempt any **two** of the following : 10×2

(a) Derive the formula

$$y'_0 = (y_{-2} - 8y_{-1} + 8y_1 - y_2) / 12h$$

For numerical differentiation at mid-point of a table, and indicate the truncation error.

(b) Derive Simpson's 3/8th rule on integration.

Hence, evaluate $\int_0^6 \frac{1}{1+x} dx$.

(c) Evaluate the value of the integral

$$\int_{.2}^{1.4} (\sin x - \log_e x + e^x) dx \text{ by}$$

Weddle's rule.

4 Attempt any two of the following : 10×2

(a) If $\frac{dy}{dx} = x + y^2$, use Runge-Kutta method of

fourth order to find an approximate value of y for $x = 0.2$, given that $y = 1$ when $x = 0$.

(b) Apply predictor-corrector method, find $y(2)$ if

$y(x)$ is the solution of $\frac{dy}{dx} = \frac{1}{2}(x + y)$ given

$$y(0) = 2, y(.5) = 2.636 \quad y(1) = 3.595 \text{ and}$$

$$y(1.5) = 4.968.$$

(c) Applying Euler's method to the equation

$$\frac{dy}{dx} = -y, \text{ given } y(x_0) = y_0, \text{ determine its}$$

stability zone ?

5 Attempt any two of the following : 10×2

(a) Fit a second degree parabola to the data, taking y as dependent variable :

$x :$	1929	1930	1931	1932	1933	1934	1935
$y :$	352	356	357	358	360	361	361

(b) Find the multiple linear regression of X_1 on X_2 and X_3 from the data relating to three variables :

$X_1 :$	7	12	17	20
$X_2 :$	4	7	9	12
$X_3 :$	1	2	5	8

(c) In a manufacturing process, the number of defectives items found in the inspection of 15 lots of 400 items each are given below :



<i>Lot No.</i>	<i>No. of defective</i>	<i>Lot No.</i>	<i>No. of defective</i>
1	2	9	18
2	5	10	8
3	0	11	6
4	14	12	0
5	3	13	3
6	0	14	0
7	1	15	6
8	0		

Determine the trial control limits for np chart and state whether the process is in control

