



(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 9967Roll No. **B. Tech.****(SEM. III) EXAMINATION, 2007-08
COMPUTER BASED NUMERICAL AND
STATISTICAL TECHNIQUES**

Time : 3 Hours]

[Total Marks : 100

*Note : Attempt all questions. All questions carry equal marks.***1** Attempt any four parts of the following : **5×4=20**

- (a) State the most common and popular computer arithmetic systems. Discuss with examples that the distributive laws of floating point arithmetic is not always satisfied in numerical computing.
- (b) Use the series

$$\log_e \left(\frac{1+x}{1-x} \right) = 2 \left(x + \frac{x^3}{3} + \frac{x^5}{5} + \dots \right)$$

to compute the value of $\log_e(1.2)$ correct to seven decimal places and find the number of terms retained.

- (c) In a triangle ABC , $a = 30 \text{ cm}$, $b = 80 \text{ cm}$, $\angle B = 90^\circ$. Write a program in 'C' to find the maximum possible error in the computed value of area of ΔABC , if possible errors in a and b are $\frac{1}{3}\%$ and $\frac{1}{4}\%$ respectively.

- (d) Develop an iteration formula to find a real root of the equation :

$$10 \int_0^x e^{-x^2} dx = 1.$$

Find a root of this equation in the interval $(0, 1)$.

- (e) Find a real root of the following equation correct to 3 decimal places $\cos x - xe^x = 0$ by Bisection method.
- (f) Find a positive value of $\sqrt{13}$ correct to 4 decimal places by Newton-Raphson method.

2 Attempt any four parts of the following :

- (a) (1) Prove : $\Delta + \nabla = \Delta / \nabla - \nabla / \Delta$.
- (2) Find the missing term in the table :

$x :$	2	3	4	5	6
$f(x) :$	45.0	49.2	54.1	?	67.4

- (b) Find the polynomial interpolating the data :

$x :$	0	1	2
$f(x) :$	0	5	2

Hence estimate $\max |f(x)|$ in $[0, 2]$ and the value of $\int_0^2 f(x) dx$.

- (c) State rules to find the suitable formula for interpolating the data.
- (d) Using the Newton's divided difference formula find a polynomial which takes the values 3, 12, 15, -21, when x has the values 3, 2, 1, -1, respectively.

(e) For the following data :

x	$f(x)$	$f'(x)$
0.5	4	-16
1	1	-2

find the Hermite interpolating polynomial, fitting the data.

(f) Calculate the value of $f(1.5)$ using Bessel's interpolation formula :

$x :$	0	1	2	3
$f(x) :$	3	6	12	15

3 Attempt any two parts of the following :

(a) When does the need of numerical differentiation arise ?
Given the following data, find $y'(6)$

$x :$	0	2	3	4	7	8
$y :$	4	26	58	112	466	922

(b) State the need and scope of numerical integration. Use the trapezoidal rule to estimate the integral

$$\int_0^2 e^{x^2} dx$$

taking the number of intervals 10.

(c) Derive an expression for error estimation in Simpson's one-third rule. Use Boole's five-point formula to compute

$$\int_0^{\pi/2} \sqrt{\sin x} dx.$$

4 Attempt any two parts of the following :

(a) Given the initial value problem :

$$y' = 1 + y^2, \quad y(0) = 0.$$

find $y(0.6)$ by Runge-Kutta method taking $h = 0.2$.

(b) Write a program in 'C' to solve the initial value problem :

$$y' = (x^2 - 1)y^2, \quad y(0) = 2, \quad 0 \leq x \leq 1$$

by Milne's Predictor-Corrector method.

(c) (1) Discuss the stability of Euler's method applied to the initial-value problem

$$y' = \lambda y, \quad y(0) = 1$$

(2) Consider the initial value problem :

$$y' = 2x + 3y, \quad y(0) = 1$$

Determine the number of terms in the Taylor's series required to obtain results correct to 5×10^{-6} for $x \leq 0.4$.

5 Attempt any two parts of the following :

(a) State some important curve-fitting procedures. Obtain the least squares fit of the form

$$f(t) = ae^{-3t} + be^{-2t} \text{ for the data :}$$

t	0.1	0.2	0.3	0.4
$f(t)$	0.76	0.58	0.44	0.35

(b) Discuss regression and its importance. Given the following data : <https://www.aktuonline.com>

$x :$	1	5	3	2	1	1	7	3
$y :$	6	1	0	0	1	2	1	5

Find a regression line of x on y .

(c) Discuss how control charts can be used in quality control of industrial products. The average percentage of defectives in 27 samples of size 1500 each was found to be 13.7%. Construct a suitable control chart for this problem. Explain how the control chart can be used to control quality.