

(Following Paper ID and Roll No. to be filled in your Answer Book)

PAPER ID : 9967

Roll No.

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B.Tech.

THIRD SEMESTER EXAMINATION, 2005-2006

**COMPUTER BASED NUMERICAL AND
STATISTICAL TECHNIQUES**

Time : 3 Hours

Total Marks : 100

- Note :** (i) Attempt ALL questions.
(ii) All questions carry equal marks.
(iii) In case of numerical problems assume data wherever not provided.
(iv) Be precise in your answer.

1. Attempt any four parts of the following : (5x4=20)

- (a) Let x^* approximate x correct upto n significant digits if e^x is evaluated for x , $-8 \leq x \leq 9$, then what should be relative error ?
- (b) Obtain polynomial approximation to $f(x) = (1-x)^{1/2}$ over $[0, 1]$, by means of Taylor expansion about $x=0$. Find the number of terms required in the expansion to obtain results correct to 5×10^{-1} for $0 \leq x \leq 1/2$.
- (c) Find a real root of the equation $x^3 + x^2 - 1 = 0$ on the interval $[0, 1]$ with an accuracy of 10^{-4} by the iteration method.
- (d) Find all the roots of $\cos x - x^2 - x = 0$ to five decimal places by Newton-Raphson method.

- (e) Show that the following sequence has convergence of the second order with the same limit \sqrt{a}

$$x_{n+1} = \frac{1}{2} x_n \left(3 - \frac{x_n^2}{a} \right).$$

- (f) Do two iteration of Muller's method to solve $x^3 - 2x + 1 = 0$ starting with $x_0 = 0.5$, $x_2 = 0$, $x_1 = 1$.

2. Attempt any four parts of the following : (5x4=20)

- (a) Prove the following :

$$hD \equiv \log(1 + \Delta) = -\log(1 - \nabla) = \text{Sinh}^{-1}(\mu\delta)$$

- (b) From the following table :

x :	10°	20°	30°	40°	50°	60°	70°	80°
$\text{Cos } x$:	.9848	.9397	.8660	.7660	.6428	.5000	.3420	.1737

Calculate $\text{Cos } 25^\circ$ and $\text{Cos } 73^\circ$ using Gregory Newton formula.

- (c) Form the following table, find the value of $e^{1.17}$ using Gauss's forward formula :

x :	1.00	1.05	1.10	1.15	1.20	1.25	1.30
e^x :	2.7183	2.8577	3.0042	3.1582	3.3201	3.4903	3.6693

- (d) Using Everett's formula, evaluate $f(30)$ if $f(20) = 2854$, $f(28) = 3162$, $f(36) = 7088$, $f(44) = 7984$.
- (e) For the following table find $f(x)$ as a polynomial in x using Newton's divided difference formula.

x :	5	6	9	11
$f(x)$:	12	13	14	16

- (f) Using Lagrange interpolation formula, calculate $f(3)$ from the following table :

x :	0	1	2	4	5	6
$f(x)$:	1	14	15	5	6	19

3. Attempt *any two* parts of the following : (10x2=20)

(a) If $y=f(x)$ and y_n denotes $f(x_0+nh)$, prove that, if powers of h above h^6 be neglected,

$$\left(\frac{dy}{dx}\right)_{x=x_0} = \frac{3}{4h} \left[y_1 - y_{-1} - \frac{1}{5}(y_2 - y_{-2}) + \frac{1}{45}(y_3 - y_{-3}) \right]$$

(b) Find $\int_0^6 \frac{e^x}{1+x} dx$ approximately using Simpson's 3/8th rule on integration.

(c) Derive weddle's rule of integration. Hence, evaluate

$$\int_0^1 \frac{1}{1+x^2} dx$$

4. Attempt *any two* parts of the following : (10x2=20)

(a) Give $\frac{dy}{dx} = 1 + y^2$, where $y=0$ when $x=0$. Find $y(0.2)$, $y(0.4)$ and $y(0.6)$ by using Runge-Kutta Fourth order formula.

(b) Apply predictor-corrector method to find a solution of the differential equation $\frac{dy}{dx} = x - y^2$ in the range $0 \leq x \leq 1$ for boundary condition $y=0$ at $x=0$.

(c) Applying Euler's method to the equation $\frac{dy}{dx} = \lambda y$, given $y(x_0) = y_0$, determine its stability zone? What would be the range of stability when $\lambda = -1$?

5. Attempt *any two* parts of the following : (10x2=20)

(a) Fit a second degree parabola to the following data, taking y as dependent variable

$x :$	1	2	3	4	5	6	7	8	9
$y :$	2	6	7	8	10	11	11	10	9

(b) Find the multiple linear regression of X_1 on X_2 and X_3 from the data relating to three variables :

$X_1 :$	4	6	7	9	13	15
$X_2 :$	15	12	8	6	4	3
$X_3 :$	30	24	20	14	10	4

(c) In a factory producing spark plug the number of defectives found in inspection of 20 lots of 100 each, is given below.

Lot No	No. of defectives	Lot No	No. of defectives
1	5	11	4
2	10	12	7
3	12	13	8
4	8	14	3
5	6	15	3
6	4	16	4
7	6	17	5
8	3	18	8
9	3	19	6
10	5	20	10

Construct appropriate control chart and state whether the process is in statistical control.

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